

Present status of the investigation on the spectra of moderately charged thulium ions

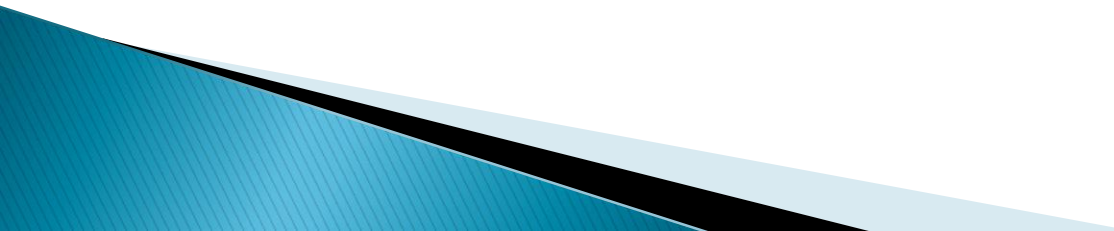
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Tribute to Jean-François Wyart

Plan

- ▶ Introduction
 - ▶ Experimental method
 - ▶ Analysis and Results
 - ▶ Conclusion
- 

Introduction

Lanthanide properties

57 La Lanthanum 138.91 [Xe] 5d ¹ 6s ²	58 Ce Cerium 140.12 [Xe] 4f ¹ 5d ¹ 6s ²	59 Pr Praseodymium 140.91 [Xe] 4f ³ 6s ²	60 Nd Neodymium 144.24 [Xe] 4f ⁴ 6s ²	61 Pm Promethium 144.91 [Xe] 4f ⁵ 6s ²	62 Sm Samarium 150.36 [Xe] 4f ⁶ 6s ²	63 Eu Europium 151.96 [Xe] 4f ⁷ 6s ²	64 Gd Gadolinium 157.25 [Xe] 4f ⁷ 5d ¹ 6s ²	65 Tb Terbium 158.93 [Xe] 4f ⁹ 6s ²	66 Dy Dysprosium 162.50 [Xe] 4f ¹⁰ 6s ²	67 Ho Holmium 164.93 [Xe] 4f ¹¹ 6s ²	68 Er Erbium 167.26 [Xe] 4f ¹² 6s ²	69 Tm Thulium 168.93 [Xe] 4f ¹³ 6s ²	70 Yb Ytterbium 173.05 [Xe] 4f ¹⁴ 6s ²	71 Lu Lutetium 174.97 [Xe] 4f ¹⁴ 5d ¹ 6s ²
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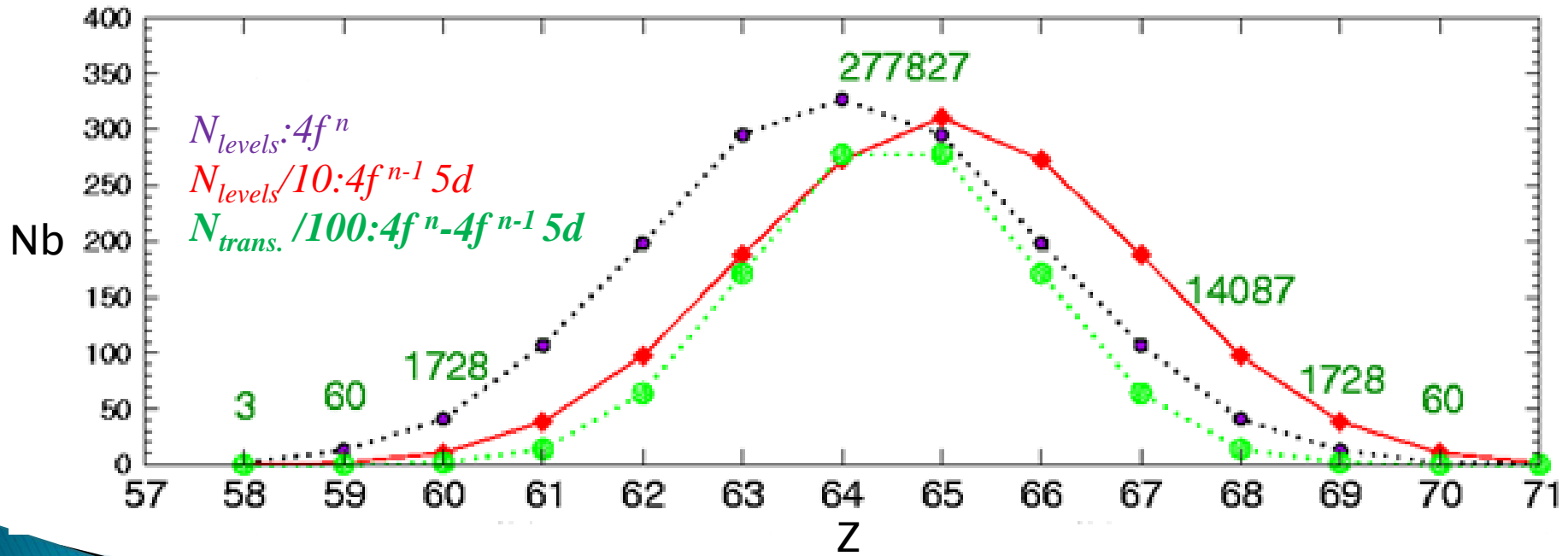
- ▶ $Z = 57 \longrightarrow 71$ with open f-shell configurations.
- ▶ 4f, 5d, 6s and 6p have similar binding energies:
 - Overlapping configurations
 - High level densities, even at a few eV

Introduction

► Lanthanides complexities:

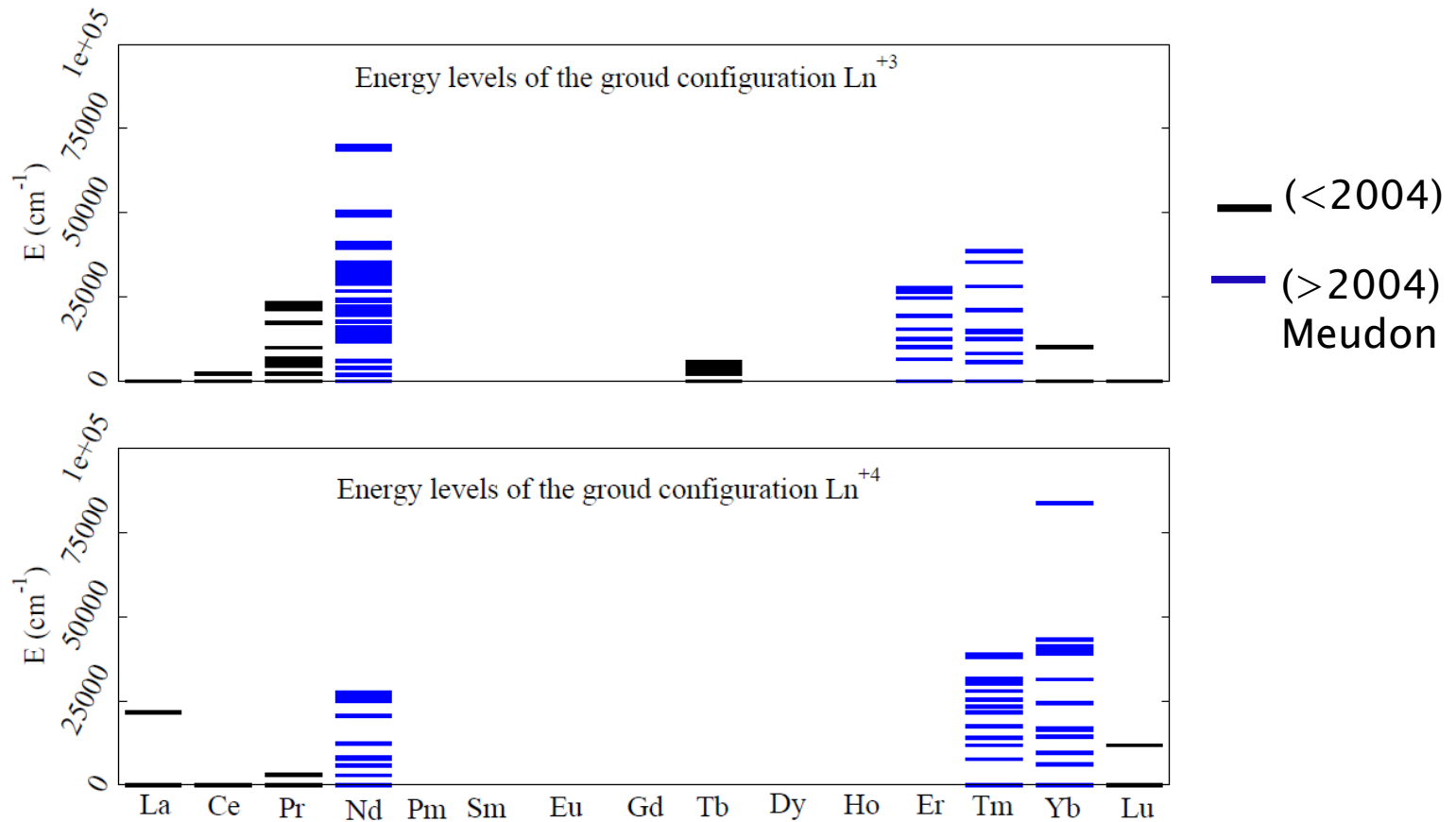
$4f^7(\text{Gd}^{3+})$: **327** levels ; $4f^75d(\text{Tb}^{3+})$: **3106** levels

$\underbrace{4f^7 - 4f^65d}_{\text{Gd}^{3+}}$; $\underbrace{4f^8 - 4f^75d}_{\text{Tb}^{3+}}$
277827 transitions



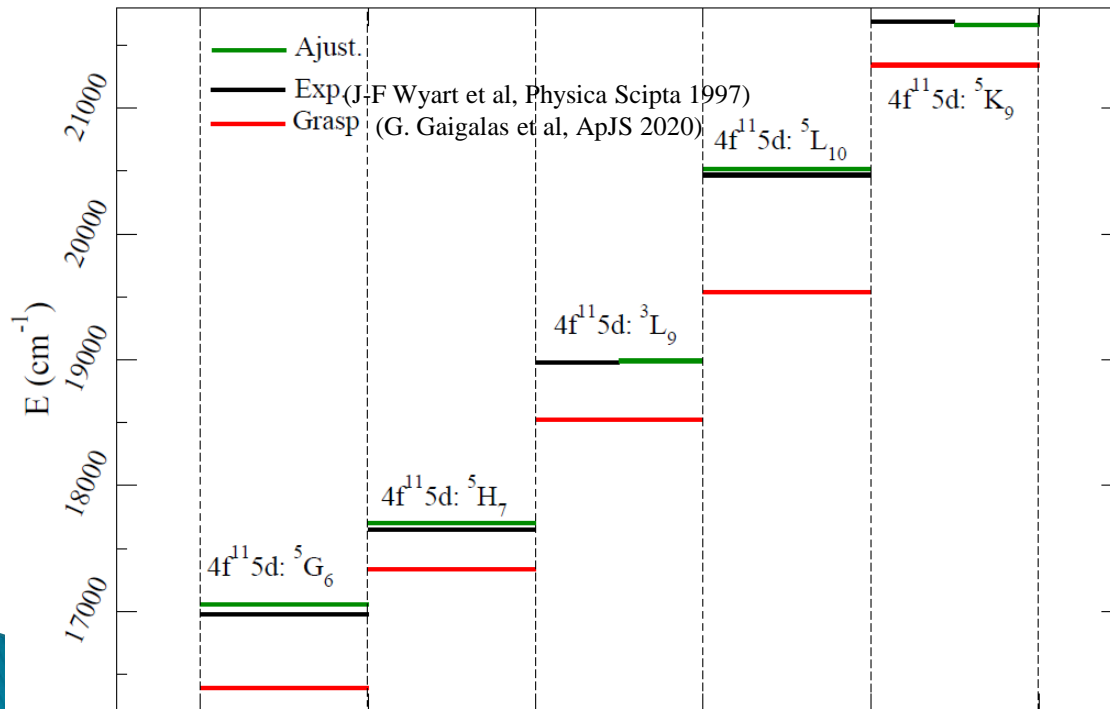
Introduction

There are very little experimental data for the lanthanide ions



Introduction

- Ab initio atomic structure codes (GRASP, FAC,...)
- *Experimental levels are very important to confirm the validity of these codes and accompany their future developments*
- In the semi-empirical approach:
 - *The values of the experimental energies allow to improve very significantly the calculated values by adjusting them with experimental value.*



Ex: Er^{2+}

first levels of $4f^{11}5d$

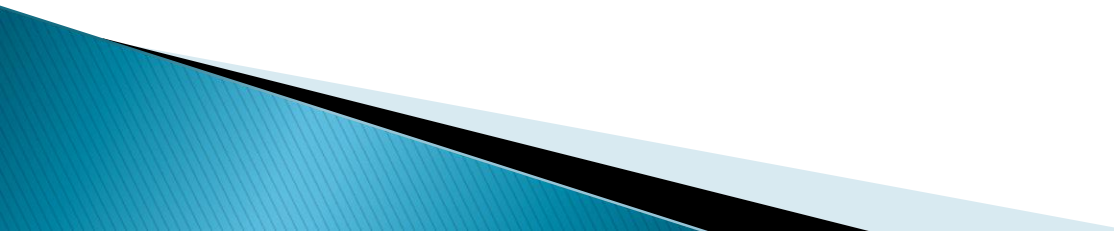
$$E_{\text{exp}} - E_{\text{Grasp}} \sim$$

a few hundred cm^{-1}

▶ $E_{\text{exp}} - E_{\text{Ajust}} \sim$

a few tens cm^{-1}

Introduction

- ▶ lanthanide ions are of interest for:
 - Luminescence of materials doped with lanthanide ions.
 - Spectra of chemically peculiar stellar atmospheres
 - Study of kilonovae (neutron-star mergers)
- 

Experimental method

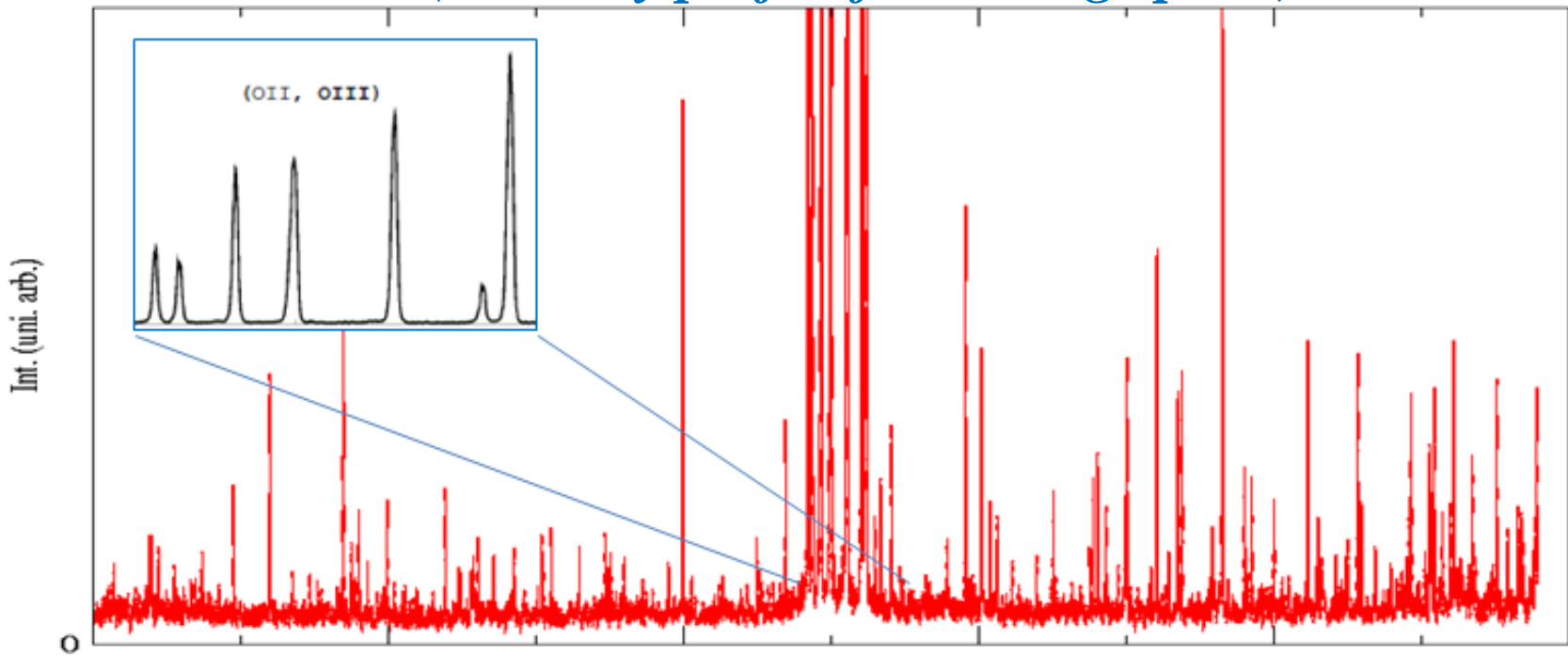
Meudon VUV spectrograph



- **Holographique Concave grating: 3600 lines/mm**
- **Focal length: 10.685 m**
- **λ of maximum efficiency: 120 nm**
- **Resolving power: $1.5 \cdot 10^5$ (8 mA, slit 30 μm)**
- **Spectral range: 30-300 nm**

Experimental method

A section of thulium sliding spark spectrum in wavelength range 810-860 Å
(Intensity profile from image plate)



- *The lines of impurities inside the spectrum are used for calibration in wavelength*

Analysis and Results

Principle of Analysis

Exp. λ (σ) list

λ_1 (σ_1)
 λ_2 (σ_2)
 λ_3 (σ_3)
.
.
.
.
 λ_n (σ_n)

+

Atomic structure calc.
codes

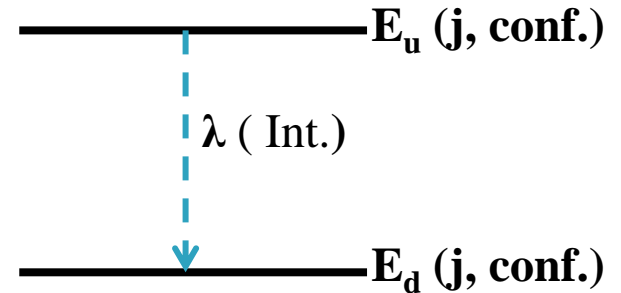
Exp. Energy levels

E_1 (j_1 , conf.)
 E_2 (j_2 , conf.)
 E_3 (j_3 , conf.)
.
.
.
.
 E_n (j_n , conf.)

=

Ritz combination principle

$$\sigma = 1/\lambda = E_u - E_d$$



Consistency between int. and gA

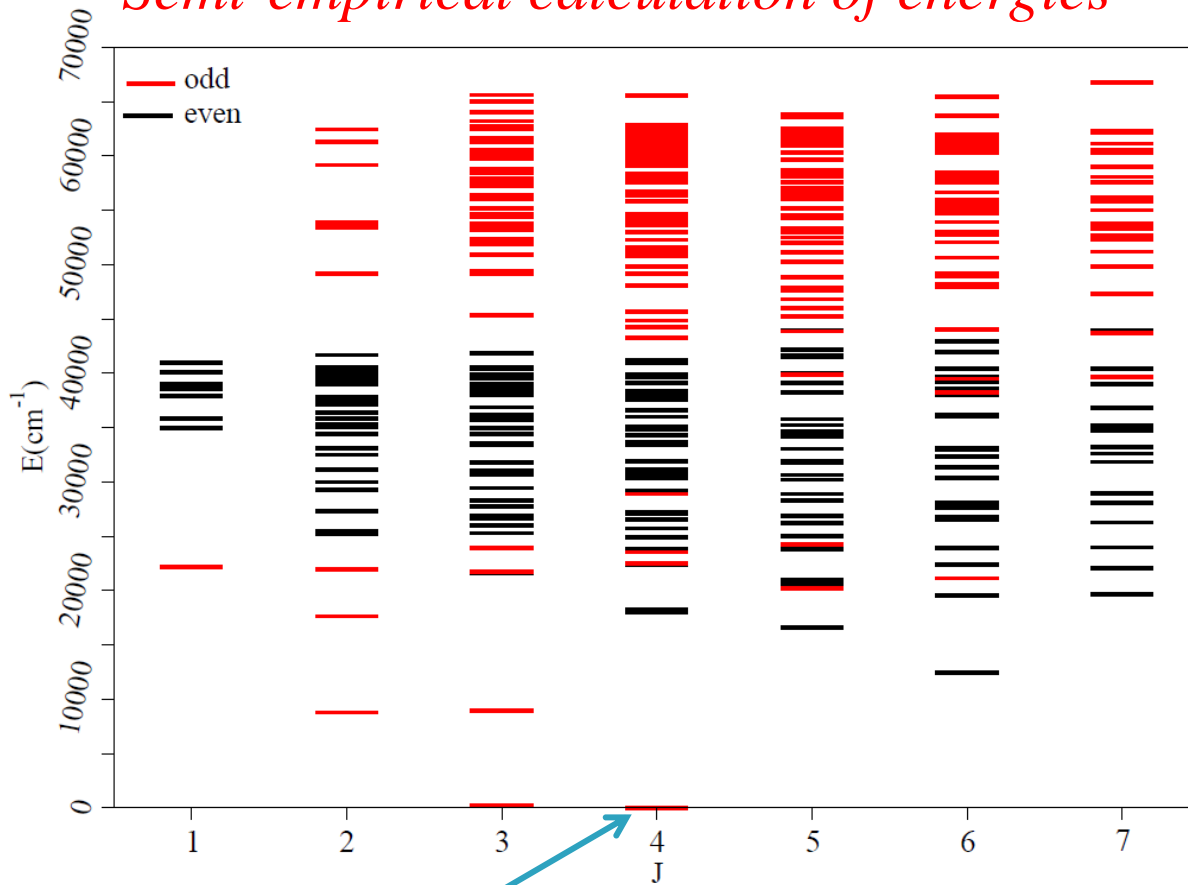
Analysis and Results

Parametric calculations: Cowan code (RCN/RCG/RCE

- ▶ *Ab initio calculations (Hartree-Fock + relativistic corrections: HFR) of the set of electronic configurations.*
- ▶ *Atomic Hamiltonian: $H = \text{radial part} \times \text{angular part}$ (Racah algebra).*
- ▶ *Least square fitting of the calculated energies by adjusting radial parameters*

Results: Tm^+

Semi-empirical calculation of energies



Ground level:
 $4f^{13}6s: {}^5F_4$

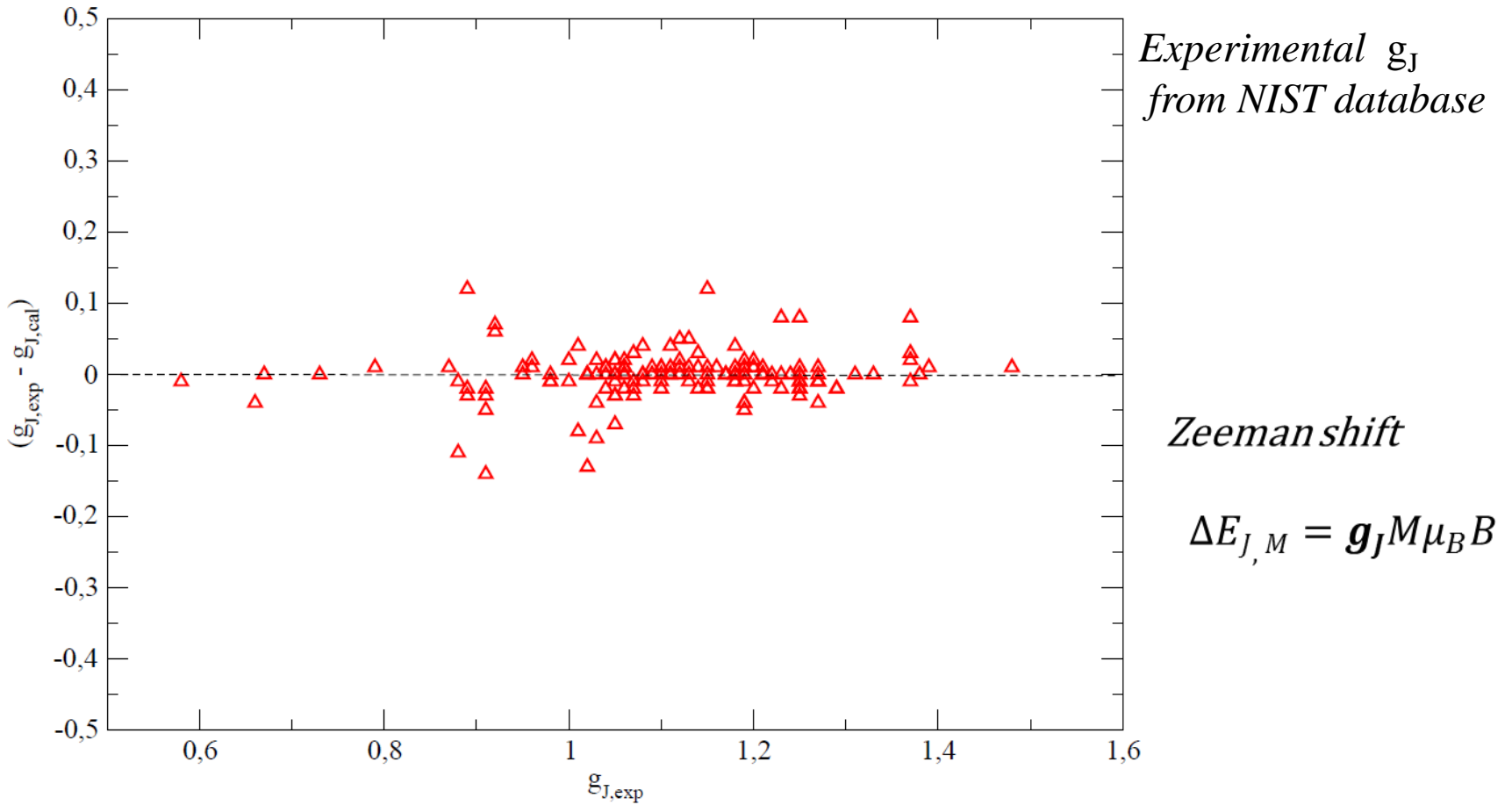
*Experimental levels
 from NIST/ASD*

Standard deviation:

$$\sigma_E = \left[\frac{\sum_{i=1}^{N_{lev}} (E_{cal,i} - E_{exp,i})^2}{N_{lev} - N_{par}} \right]^{1/2}$$

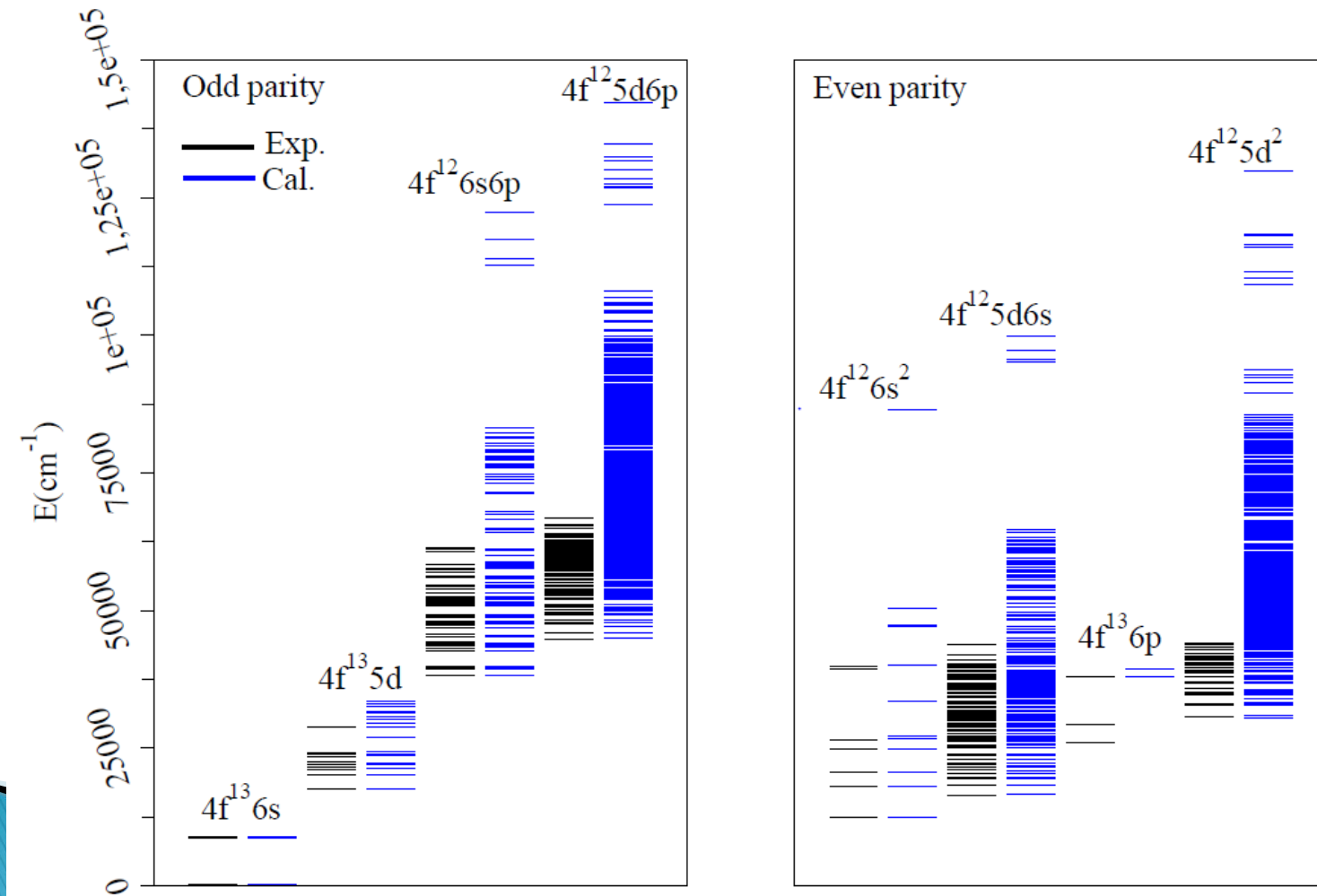
Parity	Even	odd
N_{lev}	161	182
N_{par}	23	26
$\sigma_E(\text{cm}^{-1})$	56	85

Results: Landé g_J factors calculation in Tm^{+1} comparison with measurements

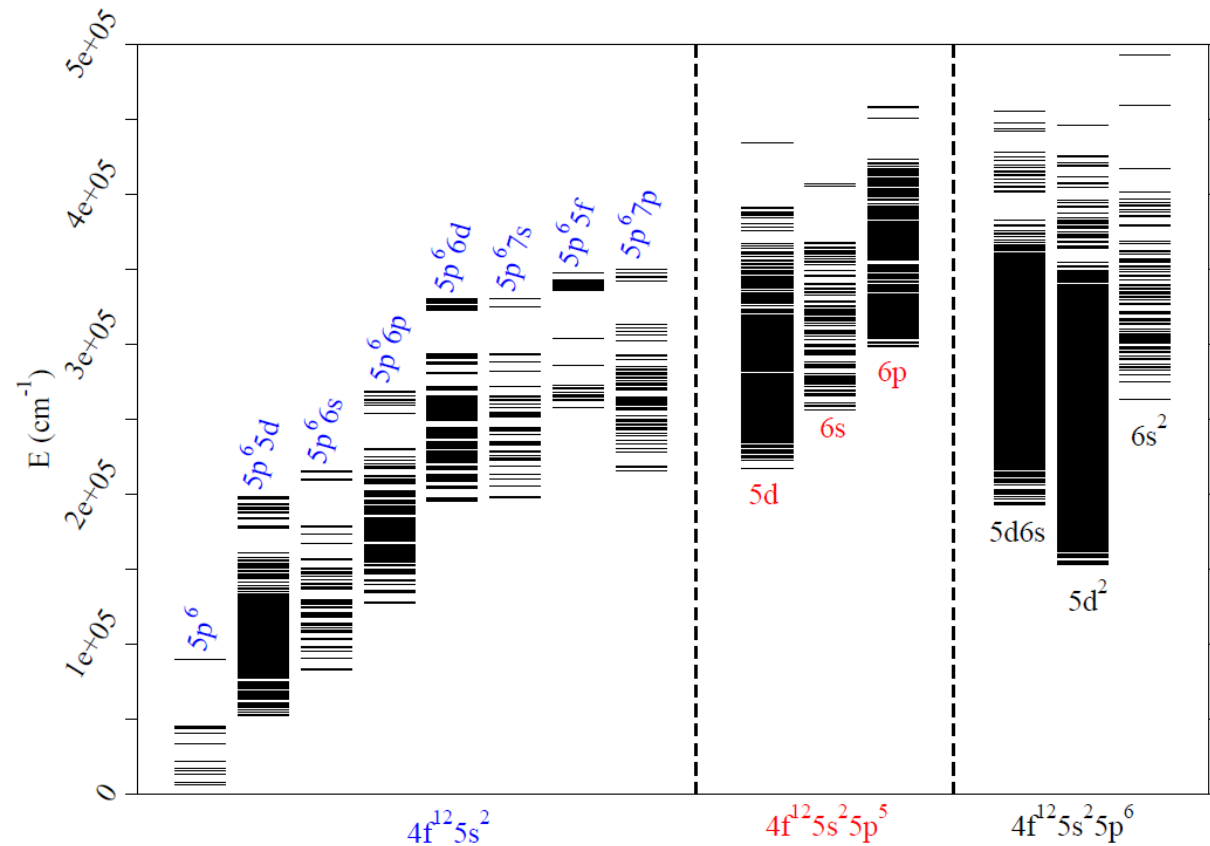


Results: Experimental and predicted levels of Tm^{+1} .

- ▶ LSQ fit with known levels improve the prediction of unknown levels



Results: Extended analyse of Tm^{3+}



- ▶ First analyse of Tm^{3+} : **209** levels

($4f^{12}$, $4f^{11} 5d$, $4f^{11} 6s$ and $4f^{11} 6p$)

(Meftah et al, EPJD 2007)

- ▶ Extended analysis: More levels for:

$4f^{12}$ → **2** new levels

$4f^{11} 5d$ → **69** new levels

$4f^{11} 6s$ → **7** new levels

$4f^{11} 6p$ → **23** new levels

Results: GRASP calculations in Tm^{3+}

- ▶ *Comparison of experimental energies (cm⁻¹) and values calculated by GRASP*

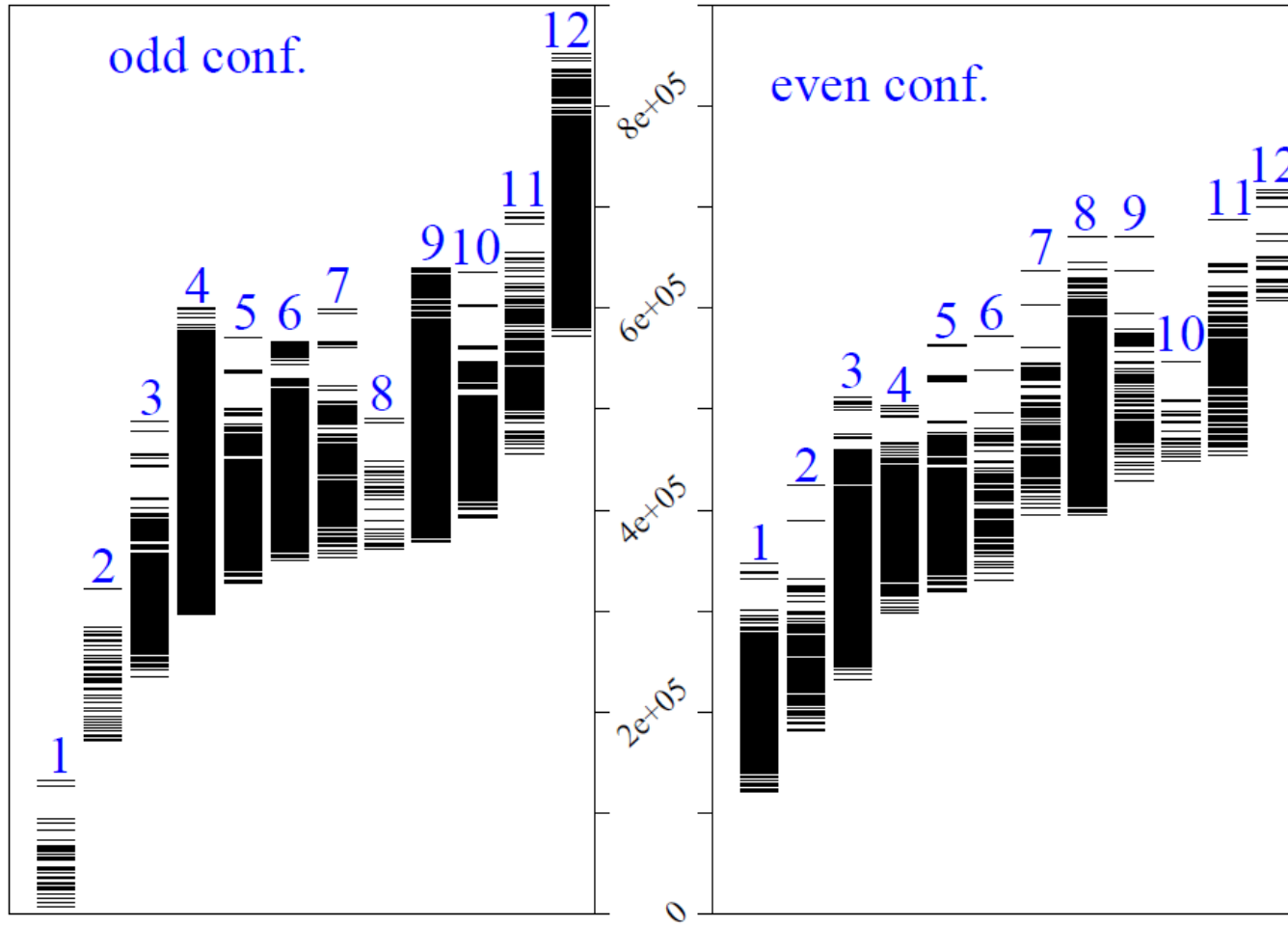
Config.	Term	J	Exp.	Ajust.	Grasp (in%)
$4f^{12}$	3H	6	0.00	-27	0
	3F	4	5634.02	5656	6571/-16.17
	3H	5	8216.73	8192	7315/10.97
$4f^{11}5d$	3H	4	12547.23	12567	11852/5.54
	3F	3	14410.41	14463	14743/-2.3
	5G	6	72011.02	72044	72145/-0.18
	5H	7	72931.67	72984	73163/-0.30
	3L	9	74506.41	74526	74735/-0.30
	5I	8	75585.02	75541	75924/-0.44
	5G	5	78413.63	78416	78286/0.16
	5K	9	78677.88	78697	78665/0.01
	5H	6	79225.87	79212	79203/0.02
	5I	8	80122.71	80116	80149/-0.03
	5I	7	80264.65	80226	80459/-0.24
	5L	8	82258.89	82261	82191/0.08
	3G	5	83293.13	83289	83613/0.38
	3I	7	83530.02	83502	83709/-0.21
	5G	4	83548.79	83549	83524/0.02
3H	6	84485.81	84438	84867/-0.45	
3G	5	85541.93	85500	85641/-0.11	
5L	9	85504.65	85524	84876/0.73	
5L	7	86145.56	86115	86157/-0.01	
$4f^{11}6s$	5I	8	98972.81	98968	100975/-2.02
	3I	7	100145.05	100138	102331/-2.18
	5I	7	106895.45	106999	108792/-1.77
$4f^{11}6p$	5I	6	107603.36	107541	109124/-1.41
	5H	7	144991.40	145008	147541/-1.75
	3K	8	145564.25	145549	148102/-1.74
	5H	6	152729.67	152740	155045/-1.51
	5K	7	153028.54	153032	155283/-1.47
	5k	9	153217.84	153227	155898/-1.75

- ▶ *Good agreement between the calculations with GRASP and the experimental values.*
- *The experimental values are reproduced to few %*
- *But not as close as the fitted values*

Results: First analyse of Tm^{4+}

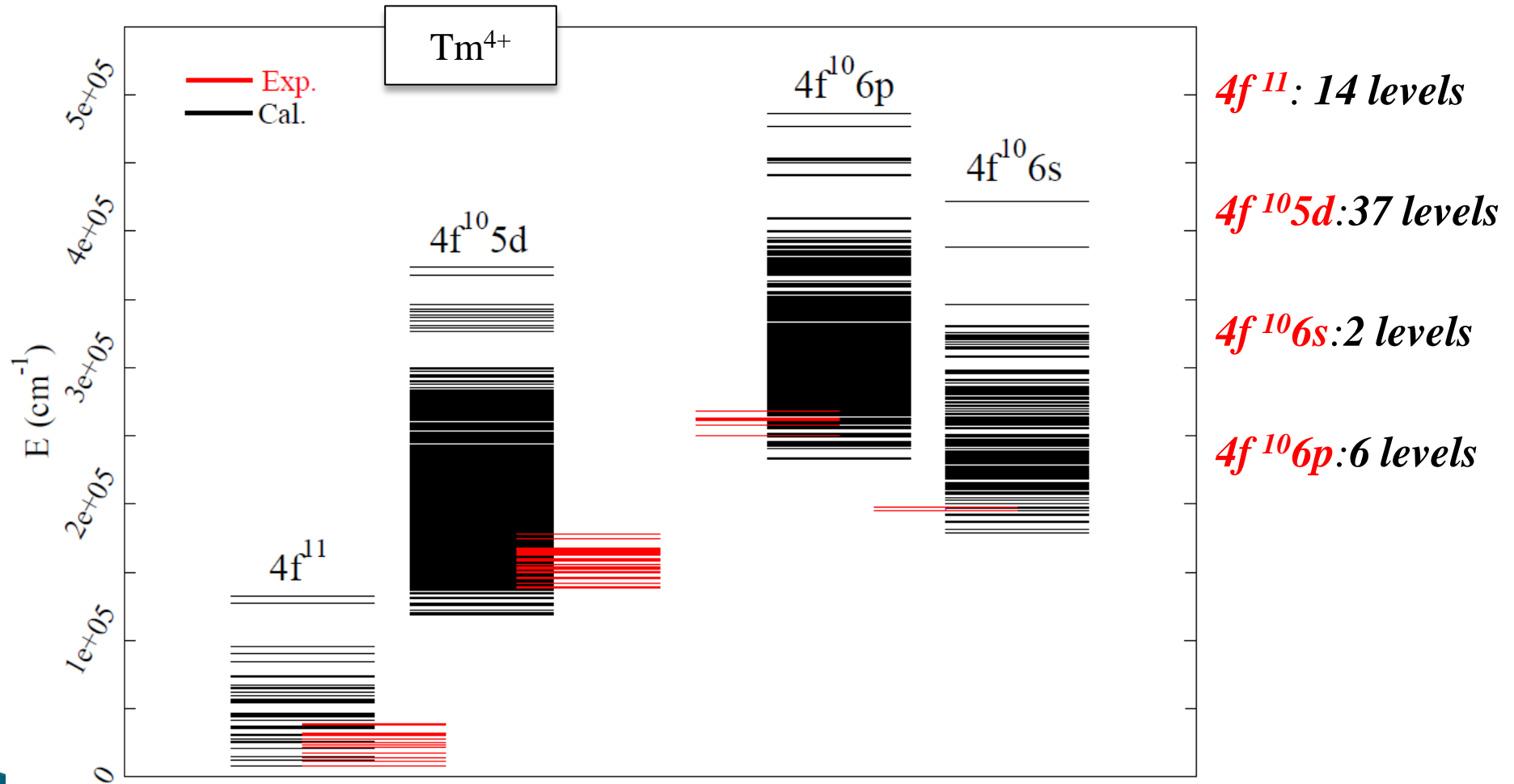
Global view of configurations

- 1: $4f^{11}$
- 2: $5p^5 4f^{12}$
- 3: $4f^{10} 6p$
- 4: $4f^9 5d^2$
- 5: $4f^{10} 5f$
- 6: $5p^5 4f^{11} 6p$
- 7: $4f^{10} 7p$
- 8: $5p^4 4f^{13}$
- 9: $4f^9 5d 6s$
- 10: $4f^{10} 6f$
- 11: $4f^9 6s^2$
- 12: $4f^9 6p^2$



- 1: $4f^{10} 5d$
- 2: $4f^{10} 6s$
- 3: $5p^5 4f^{11} 5d$
- 4: $5p^5 4f^{11} 6s$
- 5: $4f^{10} 6d$
- 6: $4f^{10} 7s$
- 7: $4f^{10} 5g$
- 8: $5p^4 4f^{12} 5d$
- 9: $4f^{10} 6g$
- 10: $5s^1 5p^6 4f^{12}$
- 11: $5p^4 4f^{12} 6s$
- 12: $5s^1 5p^5 4f^{13}$

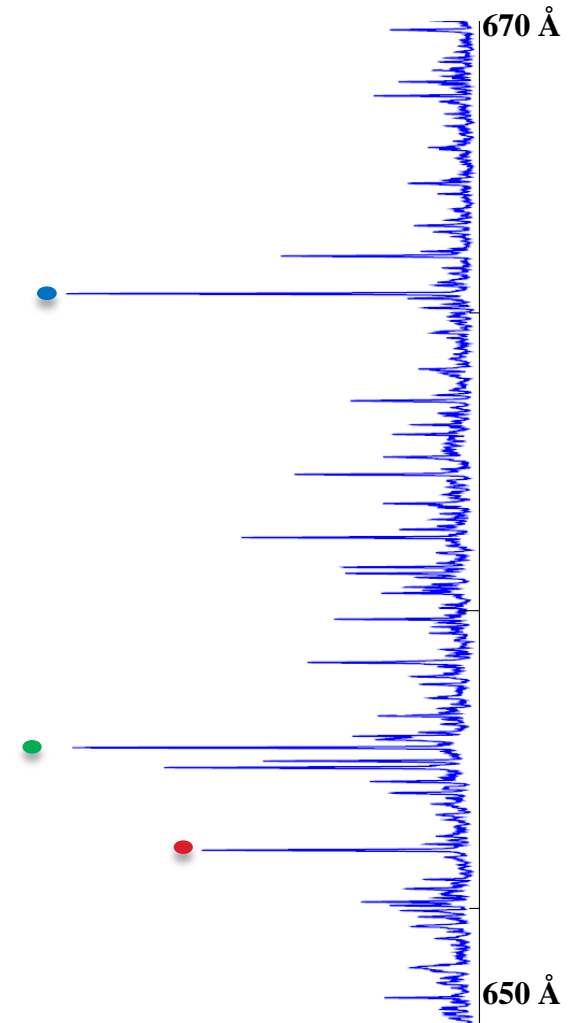
Results: First analysis of Tm^{4+}



Results: gA and gf calculations in Tm^{4+} (Tm V)

Examples of resonance lines of Tm^{4+}

E_L	Term.	J	E_u	Term.	J	$\log gf$	$gA(s^{-1})$	$\lambda(\text{\AA})$	Int.			
0.000	4I	7.5	138325.83	6H	7.5	-1.910	1.573E+08	722.931	108			
			138833.94	6I	8.5	-2.851	1.815E+07	720.283	6			
			139521.49	6G	6.5	-2.484	4.269E+07	716.731	24			
			145671.02	4K	8.5	-1.125	1.061E+09	686.478	212			
			145657.94	6H	7.5	-1.858	1.966E+08	686.539	83			
			149195.71	6L	8.5	-1.199	9.409E+08	670.259	194			
			149687.89	6K	6.5	-1.251	8.382E+08	668.055	200			
			150226.91	4I	7.5	-0.488	4.895E+09	665.659	292			
			152487.62	4I	7.5	-0.589	3.998E+09	655.790	258			
			153156.68	6K	8.5	-1.624	3.720E+08	652.924	78			
			153007.39	4H	6.5	-0.707	3.069E+09	653.562	238			
			153974.90	6L	7.5	-1.655	3.498E+08	649.454	75			
			154312.60	6H	6.5	-2.078	1.325E+08	648.034	40			
			7674.36	4I	6.5	145657.94	6H	7.5	-2.417	4.866E+07	724.727	25
						149687.89	6K	6.5	-2.057	1.179E+08	704.158	67
149824.40	6I	5.5				-2.335	6.232E+07	703.481	13			
150226.91	4I	7.5				-2.914	1.653E+07	701.498	7			
152487.62	4I	7.5				-1.277	7.381E+08	690.544	167			
153007.39	4H	6.5				-1.595	3.585E+08	688.076	142			
153938.07	6K	5.5				-2.443	5.141E+07	683.696	7			
153974.90	6L	7.5				-1.548	4.038E+08	683.526	115			
154312.60	6H	6.5				-0.920	1.720E+09	681.949	238			
154345.50	4G	5.5				-1.552	4.030E+08	681.797	143			
155725.21	6K	5.5				-1.739	2.662E+08	675.440	157			
157952.57	6F	5.5				-1.908	1.854E+08	665.432	52			
158793.04	4I	6.5				-0.898	1.924E+09	661.729	224			
159285.39	6H	6.5				-1.191	9.849E+08	659.582	160			
159515.04	4H	5.5				-0.993	1.561E+09	658.584	178			



Conclusion

- ▶ Lower levels of conf. (*f^{11} , $4f^{10}5d$, $4f^{10}6s$ and $4f^{10}6p$*) in Tm^{4+} are known, further efforts are needed to determine more excited levels.
- ▶ Explore other strategies in GRASP to further improve calculations of Tm^{3+} and Tm^{4+} .
- ▶ Predictions on Tm^{1+} will be used to determine other experimental levels.

Contributors to this work

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- ▶ [Technical support : Norbert Champion and Christophe Blaess](#)
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- ▶ and
- ▶ [Jean-François Wyart](#)
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- ▶ Associated to the Paris Observatory



Thanks for your attention

